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ARRAY PROCESSING TECHNIQUES
FOR BROADBAND ACOUSTIC BEAMFORMING

A Thesis

Submitted to the Graduate Faculty of the
University of New Orleans
in partial fulfillment of the
requirements for the degree of

Master of Science
in
The Department of Electrical Engineering

by

Ryan D. Thiel

B.S., University of New Orleans 2002

May, 2005

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ABSTRACT

Audio acquisition and recording can benefit from directional reception of the acoustic signals. Current acoustic designs of highly-directional microphones are bandwidth limited and physically large. A microphone array used in conjunction with a beamforming algorithm can acquire and spatially filter the signal, but traditionally this has suffered from limitations similar to those of the purely acoustic designs. The work presented in this paper attempts to overcome these limitations by producing and analyzing three atypical techniques for broadband beamforming. The last and most successful technique employs an algorithm which calculates the difference in group delay of the acquired signals and uses that information to determine the direction of the incoming signals as a function of frequency.

CHAPTER 1

INTRODUCTION

In film production, theater, news coverage, sports broadcasting, and nature recording, audio must be recorded from a desired source without interference from other audio sources. Placing a microphone close to the desired source is the simplest way to reduce background interference but is often impractical. Common solutions require directional microphones. Directional microphones have pickup patterns which favor on-axis and reject off-axis acoustic energy. A wide assortment of microphone pickup patterns is available ranging from omnidirectional to cardioid to super-cardioid to hyper-cardioid. In order to achieve the more extreme pickup patterns, many expensive tradeoffs with other areas of microphone performance, such as bandwidth, are made, so highly-directional microphone performance leaves much to be desired.

A highly-directional microphone placed far from the source can pick up the desired signal while reducing background interference, but highly-directional microphones of the current generation have many shortcomings. The most commonly used highly-directional microphones rely on either parabolic reflectors or acoustical tubes (shotgun microphones) developed in the 1920s and 1930s to focus on-axis or reject off-axis acoustic energy [1]. Attempts to move the sound separation from the acoustic domain to the more easily manipulated signal processing domain have been made using microphone arrays with beamforming

techniques. Using a microphone array has many advantages over an acoustic approach but, with current array processing methods, array techniques suffer from many of the same tradeoffs as the acoustic methods. Coloration of the sound, poor low frequency rejection, inconsistent pickup pattern over bandwidth, and large physical size are the drawbacks of these schemes. These drawbacks provide motivation for the search for new techniques of acquiring audio data directionally.

Due to the wide availability of low-cost, high performance digital signal processors and the versatile nature of beamforming, array processing seems the best avenue to explore. Because the current beamforming methods available suffer from some of the same drawbacks as the conventional methods for highly-directional miking, new beamforming signal processing techniques are needed. The new beamforming techniques should allow for a small array to process a large bandwidth and provide a consistent narrow beamform over the bandwidth.

This thesis documents a search for these new techniques. An overview of beamforming is presented in Chapter 2, and analyses of three attempts at new beamforming techniques are presented in Chapter 3. These include Frequency Up-Conversion (3.1), Non-Linear Decimation (3.2), and Group Delay Discrimination (3.3). Chapter 4 concludes with a discussion of the effectiveness of the developed techniques and topics for future research.

CHAPTER 2

BEAMFORMING BACKGROUND

Beamforming is a method of processing data from an array of transducers to achieve spatial filtering. The spatial filtering is used to acquire signals from a particular direction while reducing interference from another. Beamforming can be applied to either receiving or transmitting arrays and has applications in radar, sonar, communications, imaging, geophysics, astrophysics, medicine, and more [2]. The discussion here is limited to beamforming as it applies to receiving arrays.

2.1 Narrowband Beamforming

Narrowband beamforming is used when the wanted signal occupies a known narrow bandwidth. Any interference outside of that bandwidth can be reduced with a temporal (as opposed to spatial) filter. If interference is expected to occupy the same bandwidth but come from a different direction than the desired signal, a beamformer can be useful. Signals from a spatial array of sensors can be combined in such a way to enhance the signal coming from one direction and reduce signal from another. The combination of the signals, for the narrowband case, is usually a sum of weighted, phase shifted signals [3]. Differences in the weights affect the shape of the beam, and changes in phase are used to change or steer the beam to a specific direction without physically moving the array. The

weights are usually complex numbers and represent both changes in phase and magnitude. A typical narrowband array beamformer is shown in Figure 2.1.

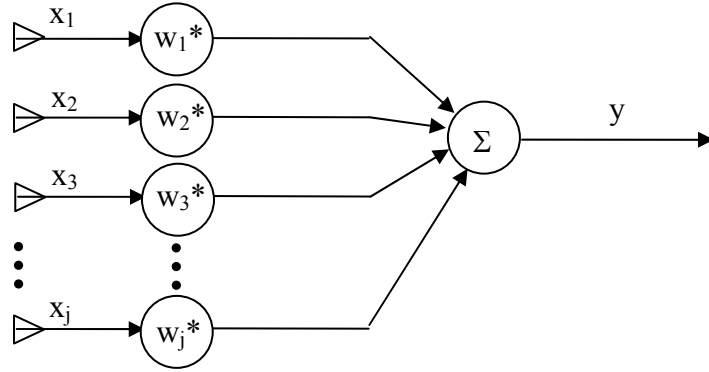


Figure 2.1. Typical Narrowband Array Beamformer

The simple two element array shown in Figure 2.2 has sensor spacing l and, on one sensor leg, has a real gain w and phase change ϕ . Figure 2.3 illustrates how the directivity pattern of the array described in Figure 2.2 is altered by changes in the gain w and phase ϕ . The source used in the example has a wavelength λ which is twice the element spacing ($\lambda = 2l$).

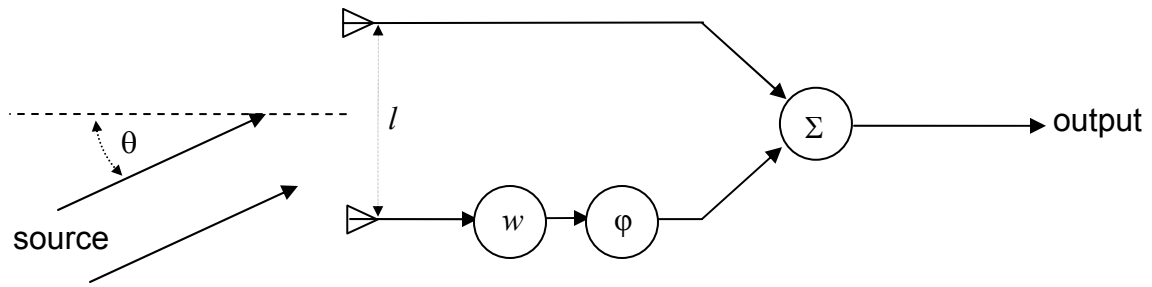


Figure 2.2. Two Element Narrowband Array and Simple Beamformer

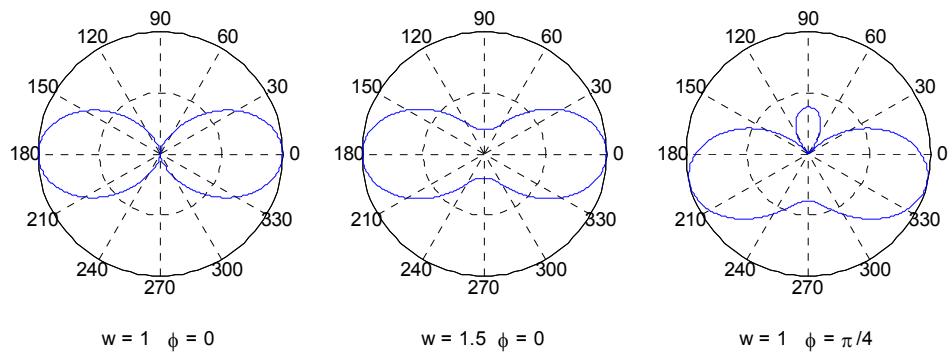


Figure 2.3. Two Element Narrowband Array Directivity Patterns

Narrowband beamformers can have many elements in any geometrical pattern. The gains of typical narrowband beamformers can be chosen to produce a wide array of beamforms. The gains can also be updated by adaptive means.

2.2 Broadband Beamforming

If the narrowband beamformer in Figure 2.2, with $w = 1$ and $\varphi = 0$, is subject to signals over a large bandwidth the beamform will change considerably. Figure 2.4 shows the directivity pattern changing drastically over a large frequency range, with wavelengths from 16 to $1/16$ times the distance between the elements, in one octave steps. This range encompasses 9 octaves which is close to the bandwidth of audio. The resulting beamforms range from nearly omnidirectional to having 64 distinct lobes.

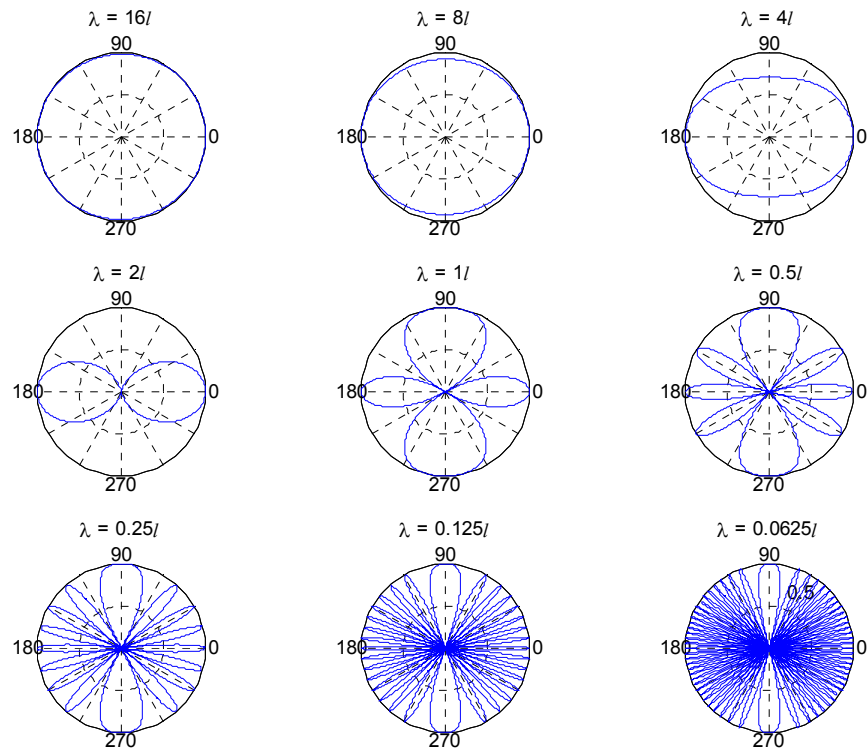


Figure 2.4. Variation of Directivity Pattern Over a Large Bandwidth

For broadband applications the desired directivity patterns remain the same over the bandwidth, so systems of the general form shown in Figure 2.1 are no longer useful. Past techniques used to help extend the bandwidth and improve the beamforming performance of an array include weighting patterns fashioned after binomial and chebyshev arithmetic schemes [4] and a method of synthesizing impulse functions[5]. A typical broadband beamformer of these types, shown in Figure 2.5, uses a finite impulse response (FIR) filter on each sensor leg before the summation. This provides the ability to change the gain and phase of the signals differently for different frequencies. Like the narrowband case, the gains can be fixed or adaptive. To accommodate the large audio bandwidth (approximately 10 octaves) the element spacing in the array must range from very small (at 20 kHz where wavelength $\lambda = 17$ mm) to very large (at 20 Hz where $\lambda = 17$ m), so an array would have to be very large and contain many elements to use this technique. This large array size is impractical in many applications, so a search for a new technique that will allow smaller array sizes (measured in physical dimensions and number of elements) begins.

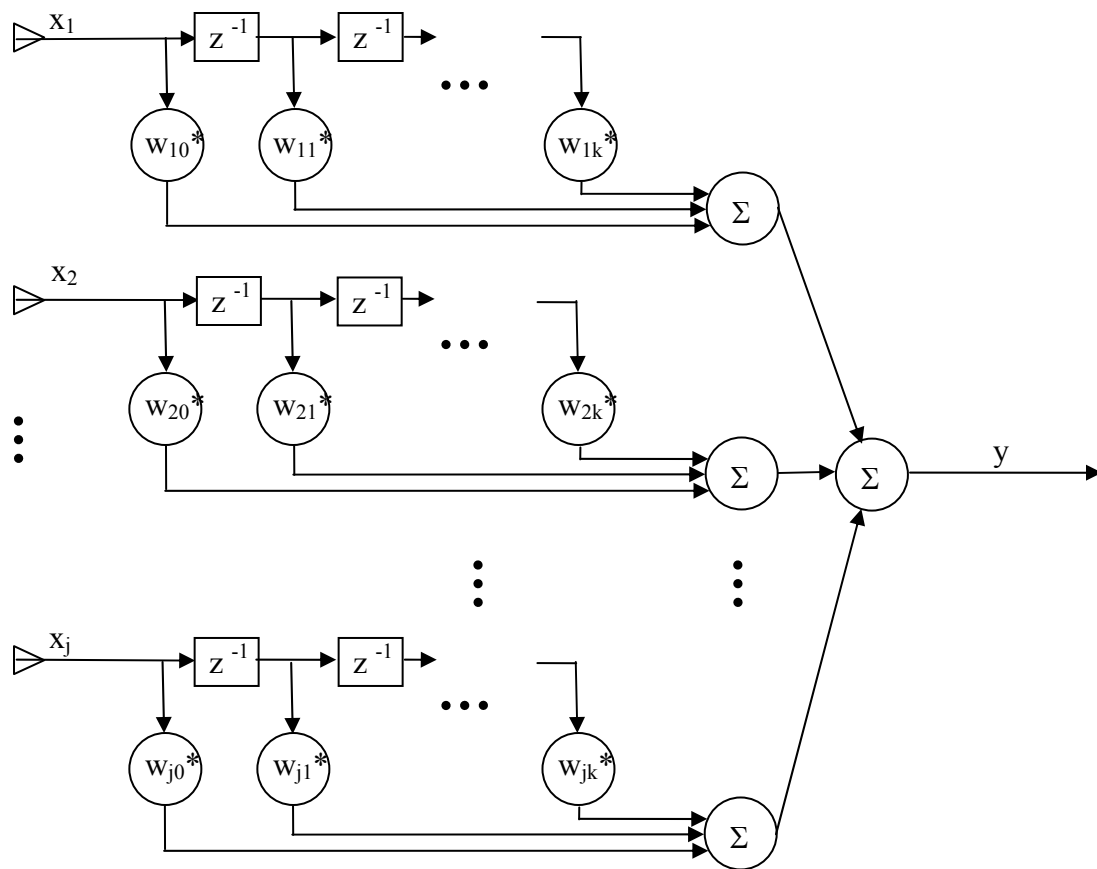


Figure 2.5. Typical Broadband Beamformer

CHAPTER 3

TECHNIQUES

The initial purpose of this thesis was to develop a broadband array processing technique for audio based on frequency up-conversion by mixing. This technique is the first discussed in this chapter. The frequency up-conversion technique did not produce the desired results so other techniques were developed and studied. The final technique, based on group-delay discrimination, produced exciting, useful results. This chapter describes each technique and its results.

3.1 Frequency Up-Conversion

3.1.1 Description

By mixing a base-band audio signal with a carrier signal much higher in frequency, the bandwidth, in octaves, of the resulting spectrum is greatly reduced. For example, a signal with frequency content from 20 Hz to 20 kHz, approximately 10 octaves, is mixed with a carrier of 100 kHz. The resulting spectrum is only 0.263 octaves wide (single sided), which appears to reduce the effective variation in wavelength and thus decrease the effective spatial variation of the signal being acquired. Can this be used to simplify the beamforming problem by effectively reducing the bandwidth and possibly reducing the required large array size? The proposed technique modulates the signal from each element

in the array by the same carrier before summation and demodulates after the summation. Filtering the lower side-band created by the modulation and using a chirp instead of a sinusoidal carrier are also considered.

3.1.2 Analysis

For an array of N elements let $x(t)$ be the source signal, so $x(t - \tau_n)$ is the signal received by array element n . For the simple case where the received signals are only summed, the resulting output $y(t) = \sum_{n=1}^N x(t - \tau_n)$. If, before the summation, the signal received at each element is mixed with a carrier $\cos(2\pi f_c t)$, the output is

$\sum_{n=1}^N [\cos(2\pi f_c t) x(t - \tau_n)]$. Because of the distributive property of multiplication, the

output of the summation simplifies to $\cos(2\pi f_c t) \sum_{n=1}^N x(t - \tau_n)$. Substituting

$y(t) = \sum_{n=1}^N x(t - \tau_n)$ yields $\cos(2\pi f_c t) y(t)$. Assuming an ideal demodulator the

output of the system is $y(t)$, the same output obtained for the simple case where the received signals are only summed. This system is illustrated in figure 3.1.

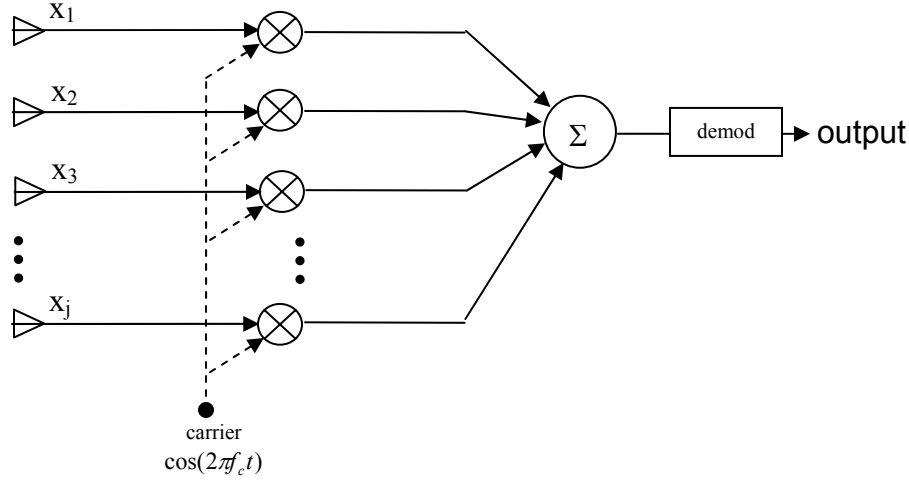


Figure 3.1. Frequency Up-Conversion Technique

An attempt to make this scheme functional by further narrowing the signal's bandwidth was made using single side-band rather than the original dual side-band modulation. Removing the lower side-band of each array element signal after modulation with a filter described by impulse function $h(t)$ yields output $\sum_{n=1}^N [(\cos(2\pi f_c t)x(t - \tau_n)) * h(t)]$ and because convolution, like multiplication, is distributive the output similarly simplifies to $h(t) * \left[\cos(2\pi f_c t) \sum_{n=1}^N x(t - \tau_n) \right]$. Substituting $y(t) = \sum_{n=1}^N x(t - \tau_n)$, yields $h(t) * [\cos(2\pi f_c t)y(t)]$. Again, assuming an ideal demodulator, the output of the system is $y(t)$, the same output obtained for the simple case where the received signals are only summed. This single side-band system is illustrated in figure 3.2.

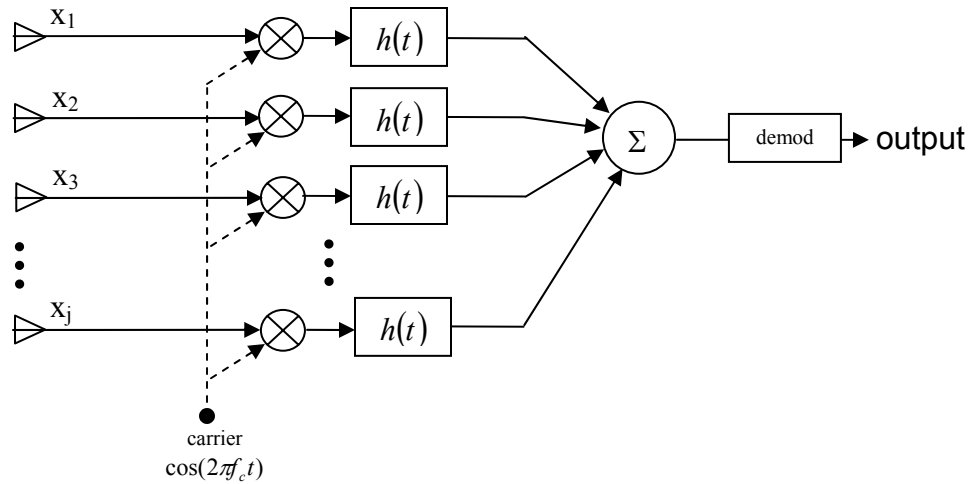


Figure 3.2. Single Side-Band Frequency Up-Conversion Technique

A third attempt was made by modulating the signals with a chirp instead of the sinusoidal carrier. The chirp technique suffers from the same problems as the other frequency up-conversion techniques, and is therefore not discussed in further detail.

3.1.3 Results

The resulting outputs of the modulated systems, when demodulated, are nothing but the output obtained by simply summing the signals from the array elements. This is due to the linear phase error characteristics of the mixing process. For example, a 2 degree phase difference between elements at 100Hz, still results in only a 2 degree phase shift at 100.1KHz after up-conversion. The hope was that low frequencies in the band which did not create enough phase shift

between receiving elements due to the long wavelengths, would experience a larger phase shift after up-conversion. This was not the case.

3.2 Non-Linear Decimation

3.2.1 Description

The non-linear decimation approach is centered on the concept of reducing the effective wavelength of a signal by removing samples in the time domain sequence. This is predicated first by the assumption that the signal is oversampled such that after decimation, the bandwidth is still usable. This approach is described in continuous time by the time scaling property of the Fourier transform

$$x(at) \Rightarrow \frac{1}{|a|} X\left(\frac{f}{a}\right)$$

where a is a real nonzero constant. If oversampling is not achieved, the problem becomes more than just a scaling operation and there can be a loss of information through aliasing.

Given there is a constant time delay for a given angle between receiving elements, that time delay will manifest itself as a phase difference. However, due to the geometry of the elements, that phase difference can be negligible at very long wavelengths. By keeping the delay the same but decimating the time sequence, a larger phase difference can be achieved. (see Figure 3.3)

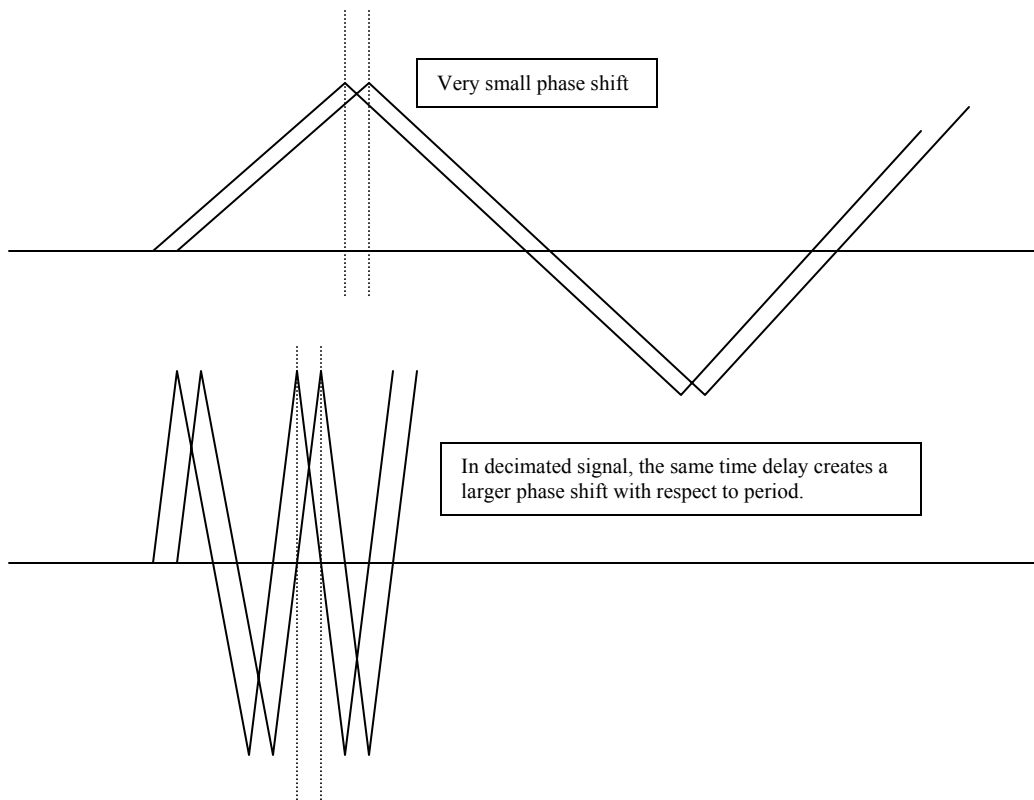


Figure 3.3 Decimation in Time

However, in order to accomplish this, there are three critical issues that are “showstoppers” for using this technique.

3.2.2 Analysis

First, there is no reduced scaling of the bandwidth with respect to octaves traversed. Section 3.1 shows how an up-conversion process could effectively reduce the relative octaves in the signal from 10 octaves to 0.263 octaves and still maintain a 20 KHz bandwidth. When linearly decimating the signal, the frequency spectrum of the signal is also shifted up but, as shown by the time scaling property, the spectrum is self-similar to the original spectrum, so there is no

reduction in octaves and there will be no improvement of the spatial variation of the array vs. frequency. This is best seen with a simple example using a square wave. A 100 Hz square wave with 50% duty cycle will have the following harmonics present: 100Hz, 300 Hz, 500Hz, 700Hz, 900Hz, etc. If the signal is sufficiently oversampled, and the samples are reduced by a factor of 10, the period is now 1/10 of what it was. The result is a square wave with a fundamental frequency of 1 KHz which contains harmonics equal to 3 KHz, 5 KHz, 7 KHz, 9 KHz, etc. The bandwidth has shifted up in frequency by a factor of 10, and more importantly, the bandwidth occupies over 3 octaves in both signals. There is no change.

Secondly, in order to use decimation to effectively increase the phase difference at long wavelengths, a non-linear process must be implemented. Blindly decimating both receiver signals does not increase the phase shift between the two receivers. Instead, a threshold must be set to mark the original position in time of the two signals and this position must be maintained. Without “moving” the signals from their original positions, the signals are then decimated from the original reference point on. (See Figure 3.4)

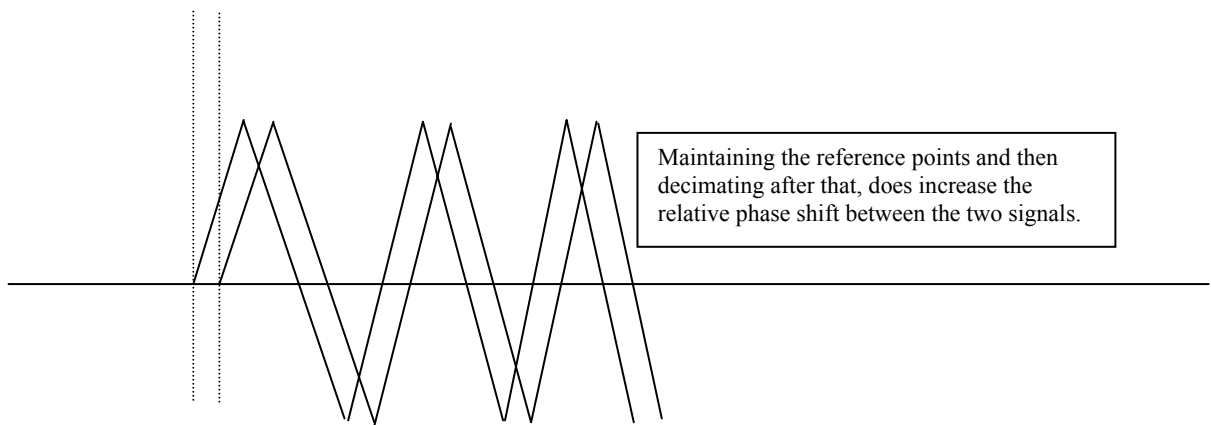
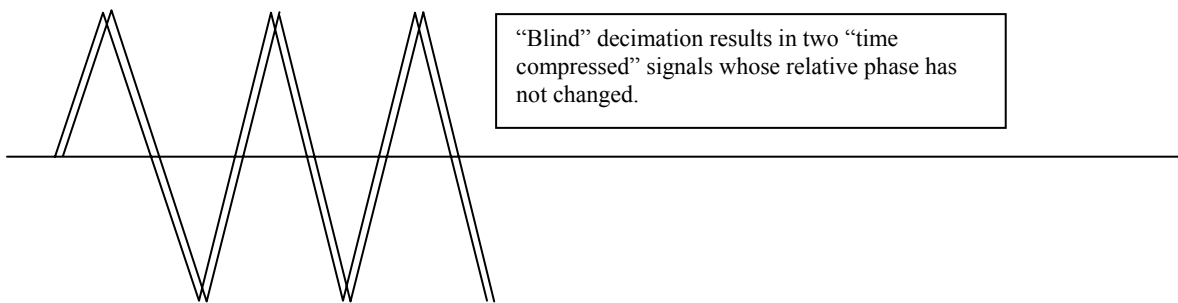
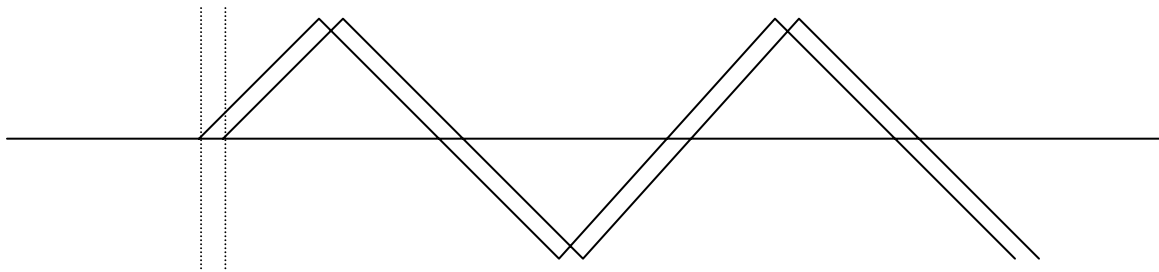


Figure 3.4 Decimation With and Without a Reference Point.

Lastly, this technique only considers one incoming signal. If more than one spatially separated, simultaneous signal is present, the algorithm breaks down. Because the reference marking algorithm would have to be based on received signal amplitude and the superposition of more than one signal causes amplitude distortion, reference marking would be unreliable. Hence, the implementation of this in a working environment such as the theater becomes unrealistic. It will be found to be much easier to differentiate simultaneous signals by their magnitude and phase responses in the frequency domain.

3.3 Group Delay Discrimination

3.3.1 Description

This technique uses the difference in group delay of the signals from two array elements to produce a temporal filter which masks frequencies contained in any off-axis interference. The filter is then applied to the signal from one element to produce the output. The filter is determined by first finding the Fourier transforms of the signals from the two array elements and expressing the transforms as a magnitude and a phase. Because the processing will be performed digitally, the discrete Fourier transform (DFT) is considered here. The forward

DFT is given by $X(k) = \sum_{n=0}^{N-1} x(n) e^{\frac{-j2\pi kn}{N}}$ and the inverse by $x(n) = \frac{1}{N} \sum_{k=0}^{N-1} X(k) e^{\frac{j2\pi kn}{N}}$.

The magnitude and phase of the DFT are notated as $|X(k)|$ and $\angle X(k)$

respectively. Group delay, as a function of frequency, can then be determined

from the phase of the transforms through differentiation with respect to angular frequency. Group delay is usually defined as the negative derivative of phase with respect to angular frequency $-\frac{d\phi}{d\omega}$ where $\phi = \angle X(\omega)$ [6]. The technique described in this chapter does not require that the group delay be the *negative* derivative, so group delay can be redefined here as $\tau(\omega) = \frac{d\phi}{d\omega}$. Because the system is discrete, an approximation of the derivative must be used. Once the group delays for the signals at each element are calculated, their difference is determined and used to define the filter's transfer function (determining the filter's transfer function is discussed in the next section). Applying the filter to the signal from either array element masks the frequency content not arriving on axis. The process is outlined in figure 3.5 and the algorithm is discussed in detail in section 3.3.2.

A technique is used in radar applications where a number of return signals are processed by two or more antenna elements, and “tagged” or characterized by their phase (incident angle) and frequency. Then an algorithm can decide which signals to prioritize and which signals to throw out if any. The similarities have to do with having the ability to determine from what direction signals of different frequencies are arriving.

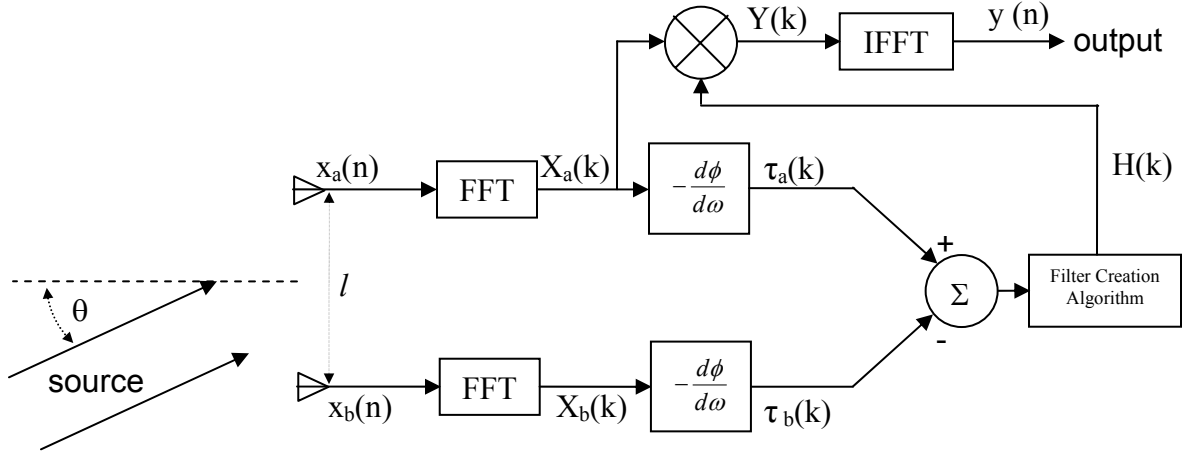


Figure 3.5. Group Delay Discrimination Process

3.3.2 Analysis

For a signal arriving at a two element array, the time delay between elements is a function of the incident angle θ and is described by the equation

$\tau = \frac{l \sin \theta}{c}$, where c is the propagation speed. The phase difference between the

two elements is a function of the angle of propagation and frequency of the signal

and is described by the equation $\phi = \frac{2\pi f l \sin \theta}{c}$. Taking the derivative of ϕ with

respect to angular frequency $\omega = 2\pi f$ gives $\frac{d\phi}{d\omega} = \frac{l \sin \theta}{c} = \tau$, the time delay shown

above. This is the group delay of the signal, and can be used to determine the

incident angle of a received signal. If more than one signal from different

directions are present, the group delay, because it is a function of frequency, can

show the direction from which the signals are coming if the frequency content of

the signals have sufficient differences.

There are three instances where cyclic phenomenon must be considered. The first is where there can be more than half of one complete wavelength of a waveform within the spacing of the array elements. The difference in phase of the waveforms at the elements is cyclic. Consider two sinusoids of the same frequency with different phase. If the phase difference between the two signals is smaller than π , no problem is encountered. Because the interest here is in the absolute phase difference between the signals and a leading or lagging relationship cannot be discerned, differences of π or more may cause problems. For example, a phase difference of 1.5π can be said to be separated by 1.5π or 0.5π . This can cause interference to masquerade as a desired signal. This problem is remedied by spacing the array elements a distance smaller than half of the smallest wavelength in the band. Placing the array elements (remember there are only two) extremely close together may limit the ability of the beamformer to notice a phase difference in signals with large wavelengths. This can be overcome by using more than two elements and letting the closely spaced elements handle the small wavelengths and the distantly spaced elements handle the large wavelengths.

The second cyclic problem also has to do with the phase of the incoming signals before the difference. This is when the phase values of a signal (not the difference in phase) wrap around as frequency increases. For instance, if the phase values of a signal at adjacent frequency samples are 0.2π apart with values of 0.9π and -0.9π , the algorithm may consider this to be a 1.8π phase shift. This is remedied by “unwrapping” the phase and is implemented by the *unwrap* command

in Matlab. The *unwrap* function removes the phase discontinuities by adding or subtracting appropriate multiples of 2π . For example the sequence

$[0.8\pi \ 0.9\pi \ -\pi \ -0.9\pi]$ unwraps to $[0.8\pi \ 0.9\pi \ \pi \ 1.1\pi]$.

The third instance of possible problem causing cyclic phenomenon has to do with the recursive nature of the DFT and the length of the signal being processed. As far as the DFT is concerned, signals in both domains repeat indefinitely in both directions. For instance, the time-domain sequence of four samples $[(1) \ 0 \ 0 \ 0]$ is actually $[\dots \ 1 \ 0 \ 0 \ 0 \ (1) \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \dots]$, so when comparing two signals it may not be clear what the time delay between them is. For example, the two sequences

$$\begin{bmatrix} \dots & 1 & 0 & 0 & 0 & (1) & 0 & 0 & 0 & 1 & 0 & 0 & 0 & \dots \\ \dots & 0 & 0 & 0 & 1 & (0) & 0 & 0 & 1 & 0 & 0 & 0 & 1 & \dots \end{bmatrix}$$

are cyclic. The impulses could be said to be separated by one *or* three samples, depending on which sequence is used as the reference. This type of ambiguity can be remedied by padding sequences of N samples with N zeros or assuring that delays of more than half of the sequence length are not possible. Zero padding the two sequences above gives the following:

$$\begin{bmatrix} \dots 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & (1) & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \dots \\ \dots 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & (0) & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & \dots \end{bmatrix}$$

The zero padding ensures that the minimum distance between impulses is the correct absolute delay, 3 samples for this example.

3.3.3 Implementation

In the first step of the algorithm, the received time domain signals are zero padded if necessary (i.e. if delays of more than half of the sequence length are possible). Then the Fourier transforms, $X_a(k)$ and $X_b(k)$, of the (possibly zero padded) signals at the elements, $x_a(n)$ and $x_b(n)$, are calculated by using the fast Fourier transform (FFT). From the results $X_a(k)$ and $X_b(k)$, the phases, $\angle X_a(k)$ and $\angle X_b(k)$, are determined. Next the group delay is to be calculated. The approximate derivative can then be calculated. (In the actual implementation, the difference in phase is calculated, and the group delay calculation is performed on this difference; mathematically the processes are the same, but performing only one approximate derivative makes the process more efficient.) The approximate derivative used in the calculation is simply the difference between adjacent points which leaves a vector with one less sample than the input. This is because the values of the approximate derivative actually fall between the discrete frequency samples of the signal. This presents a problem when doing further calculations, but the difference between the first and last points of the phase can be substituted for the “missing” sample. Placing this “extra” sample before or after the N-1 difference will dictate whether the approximate derivative is a forward or backward difference. Either can be used. The group delay difference is then fed into the filter creation algorithm.

The filter creation algorithm uses the group delay difference to determine what frequencies are wanted and which are not. A filter, $H(k)$, is created to remove those frequencies which are not wanted. Where the group delay difference is zero, the signal is arriving at the two elements at the same time, which indicates that the signal is arriving on axis (perpendicular to the line defined by the two array elements). The on axis signals are wanted; all others are not. For the calculated group delay difference, a function of frequency is created to be unity when the group delay difference is close to zero (wanted signal) and zero otherwise (unwanted signal), and the function is used as the filter.

$$H(f) = \begin{cases} 1 & \text{for } |\tau(f)| \leq \tau_{\max} \\ 0 & \text{for } |\tau(f)| > \tau_{\max} \end{cases}$$

The parameter τ_{\max} is calculated with the formula $\tau_{\max} = \frac{l \sin \theta_{\max}}{c}$ based on the desired maximum angle of the beamform θ_{\max} . The directivity pattern will ideally be one between $-\theta_{\max}$ and θ_{\max} and zero otherwise. The filter creation algorithm described is certainly not the only method that can be used. Any function of the group delay difference may be used to produce other beamforms.

The filter is then applied to the signal from one of the elements. Because the filter is described by its transfer function and the Fourier transform of the incoming signal has been determined, the filter is implemented by multiplication in the frequency domain. The inverse Fourier transform of the product is

performed and the result is truncated (because of the zero padding in the first step) yielding the output of the system $y(n)$.

This technique can be implemented in near real time if small adjacent time frames are processed serially. The number of samples should be large enough to have adequate resolution in the frequency domain.

3.3.4 Results

The algorithm was implemented in MATLAB and first tested with the following parameters:

Sampling Frequency $f_s = 8$ Hz
Number of Samples $N = 4$
Element Spacing $l = 1$
Maximum Incident Angle $\theta_{\max} = 10.8^\circ$
Propagation Speed $c = 1$

One incoming signal is considered; it is a discrete impulse $[(1 \ 0 \ 0 \ 0)]$.

Four incident angles θ are considered which are $\theta = 0^\circ$, $\theta = 7.18^\circ$, $\theta = 14.477^\circ$, and $\theta = 22.024^\circ$. The angles are chosen to create delays of 0, 1, 2, and 3 samples respectively. The maximum incident angle $\theta_{\max} = 10.8^\circ$ corresponds to a time delay which falls between 2 and 3 samples. Therefore, the incident angles $\theta = 0^\circ$ and $\theta = 7.18^\circ$ should return the signal and the incident angles $\theta = 14.477^\circ$ and $\theta = 22.024^\circ$ should reject the signal. For each of the four incident angles θ , a step by step walkthrough of the algorithm is shown.

Incoming Signal Parameters:

Incoming signal $x = [(1) \ 0 \ 0 \ 0]$

Incident Angles $\theta = 0^\circ, \theta = 7.18^\circ, \theta = 14.477^\circ$, and $\theta = 22.024^\circ$

For incident angle $\theta = 0^\circ$.

The signals at the elements are

$$x_a = [(1) \ 0 \ 0 \ 0]$$

$$x_b = [(1) \ 0 \ 0 \ 0]$$

Padding with N zeros

$$x_{ap} = [(1) \ \mathbf{0} \ \mathbf{0} \ \mathbf{0} \ 0 \ 0 \ 0 \ 0]$$

$$x_{bp} = [(1) \ \mathbf{0} \ \mathbf{0} \ \mathbf{0} \ 0 \ 0 \ 0 \ 0]$$

Performing the FFT

$$X_{ap} = [(1) \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1]$$

$$X_{bp} = [(1) \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1]$$

Calculating phase and the phase difference

$$\angle X_{ap} = [(0) \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$$

$$\angle X_{bp} = [(0) \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$$

$$\angle X_{ap} - \angle X_{bp} = [(0) \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$$

Calculating the group delay difference

$$\tau = [0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$$

Creating the filter

$$H = [1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1]$$

Implementing the filter

$$X_{ap} \times H = Y_p = [(1) \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1]$$

Performing the IFFT

$$y_p = [(1) \ \mathbf{0} \ \mathbf{0} \ \mathbf{0} \ 0 \ 0 \ 0 \ 0]$$

Removing the extra N samples yields the desired result.

$$y = [(1) \ \mathbf{0} \ \mathbf{0} \ \mathbf{0}]$$

For incident angle $\theta = 7.18^\circ$.

The signals at the elements are

$$\begin{aligned} x_a &= [(1) \ 0 \ 0 \ 0] \\ x_b &= [(0) \ 1 \ 0 \ 0] \end{aligned}$$

Padding with N zeros

$$\begin{aligned} x_{ap} &= [(1) \ \mathbf{0} \ \mathbf{0} \ \mathbf{0} \ 0 \ 0 \ 0 \ 0] \\ x_{bp} &= [(\mathbf{0}) \ \mathbf{1} \ \mathbf{0} \ \mathbf{0} \ 0 \ 0 \ 0 \ 0] \end{aligned}$$

Performing the FFT

$$\begin{aligned} X_{ap} &= [(1) \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1] \\ X_{bp} &= \begin{bmatrix} (1) & \frac{(1-j1)}{\sqrt{2}} & -j1 & \frac{(-1-j1)}{\sqrt{2}} & -1 & \frac{(-1+j1)}{\sqrt{2}} & j1 & \frac{(1+j1)}{\sqrt{2}} \end{bmatrix} \end{aligned}$$

Calculating phase and the phase difference

$$\begin{aligned} \angle X_{ap} &= [(0) \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0] \\ \angle X_{bp} &= \begin{bmatrix} (0) & -\frac{\pi}{4} & -\frac{\pi}{2} & -\frac{3\pi}{4} & -\pi & -\frac{5\pi}{4} & -\frac{3\pi}{2} & -\frac{7\pi}{4} \end{bmatrix} \end{aligned}$$

$$\angle X_{ap} - \angle X_{bp} = \begin{bmatrix} (0) & \frac{\pi}{4} & \frac{\pi}{2} & \frac{3\pi}{4} & \pi & \frac{5\pi}{4} & \frac{3\pi}{2} & \frac{7\pi}{4} \end{bmatrix}$$

Calculating the group delay difference

$$\tau_1 = \begin{bmatrix} \frac{1}{8} & \frac{1}{8} & \frac{1}{8} & \frac{1}{8} & \frac{1}{8} & \frac{1}{8} & \frac{1}{8} & \frac{1}{8} \end{bmatrix}$$

Creating the filter

$$H = [1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1]$$

Implementing the filter

$$X_{ap} \times H = Y_p = [(1) \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1]$$

Performing the IFFT

$$y_p = [(1) \ \mathbf{0} \ \mathbf{0} \ \mathbf{0} \ 0 \ 0 \ 0 \ 0]$$

Removing the extra N samples yields the desired result.

$$y = [(1) \ \mathbf{0} \ \mathbf{0} \ \mathbf{0}]$$

For incident angle $\theta = 14.477^\circ$.

The signals at the elements are

$$\begin{aligned}x_a &= [(1) \ 0 \ 0 \ 0] \\x_b &= [(0) \ 0 \ 1 \ 0]\end{aligned}$$

Padding with N zeros

$$\begin{aligned}x_{ap} &= [(1) \ \mathbf{0} \ \mathbf{0} \ \mathbf{0} \ 0 \ 0 \ 0 \ 0] \\x_{bp} &= [(\mathbf{0}) \ \mathbf{0} \ \mathbf{1} \ \mathbf{0} \ 0 \ 0 \ 0 \ 0]\end{aligned}$$

Performing the FFT

$$\begin{aligned}X_{ap} &= [(1) \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1] \\X_{bp} &= [(1) \ -j1 \ -1 \ j1 \ 1 \ -j1 \ -1 \ j1]\end{aligned}$$

Calculating phase and the phase difference

$$\begin{aligned}\angle X_{ap} &= [(0) \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0] \\ \angle X_{bp} &= \left[(0) \ -\frac{\pi}{2} \ -\pi \ -\frac{3\pi}{2} \ -2\pi \ -\frac{5\pi}{2} \ -3\pi \ -\frac{7\pi}{2} \right] \\ \angle X_{ap} - \angle X_{bp} &= \left[(0) \ \frac{\pi}{2} \ \pi \ \frac{3\pi}{2} \ 2\pi \ \frac{5\pi}{2} \ 3\pi \ \frac{7\pi}{2} \right]\end{aligned}$$

Calculating the group delay difference

$$\tau_1 = \left[\frac{1}{4} \ \frac{1}{4} \ \frac{1}{4} \ \frac{1}{4} \ \frac{1}{4} \ \frac{1}{4} \ \frac{1}{4} \ \frac{1}{4} \right]$$

Creating the filter

$$H = [0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$$

Implementing the filter

$$X_{ap} \times H = Y_p = [0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$$

Performing the IFFT

$$y_p = [(\mathbf{0}) \ \mathbf{0} \ \mathbf{0} \ \mathbf{0} \ 0 \ 0 \ 0 \ 0]$$

Removing the extra N samples yields the desired result.

$$y = [(\mathbf{0}) \ \mathbf{0} \ \mathbf{0} \ \mathbf{0}]$$

For incident angle $\theta = 22.024^\circ$

The signals at the elements are

$$\begin{aligned}x_a &= [(1) \ 0 \ 0 \ 0] \\x_b &= [(0) \ 0 \ 0 \ 1]\end{aligned}$$

Padding with N zeros

$$\begin{aligned}x_{ap} &= [(1) \ \mathbf{0} \ \mathbf{0} \ \mathbf{0} \ 0 \ 0 \ 0 \ 0] \\x_{bp} &= [(\mathbf{0}) \ \mathbf{0} \ \mathbf{0} \ \mathbf{1} \ 0 \ 0 \ 0 \ 0]\end{aligned}$$

Performing the FFT

$$\begin{aligned}X_{ap} &= [(1) \ 1 \ 1 \ 1 \ 1 \ 1 \ 1 \ 1] \\X_{bp} &= \begin{bmatrix} (1) & \frac{(-1-j1)}{\sqrt{2}} & j1 & \frac{(1-j1)}{\sqrt{2}} & -1 & \frac{(1+j1)}{\sqrt{2}} & -j1 & \frac{(-1+j1)}{\sqrt{2}} \end{bmatrix}\end{aligned}$$

Calculating phase and the phase difference

$$\begin{aligned}\angle X_{ap} &= [(0) \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0] \\ \angle X_{bp} &= \begin{bmatrix} (0) & -\frac{3\pi}{4} & -\frac{3\pi}{2} & -\frac{9\pi}{4} & -3\pi & -\frac{15\pi}{4} & -\frac{9\pi}{2} & -\frac{21\pi}{4} \end{bmatrix} \\ \angle X_{ap} - \angle X_{bp} &= \begin{bmatrix} (0) & \frac{3\pi}{4} & \frac{3\pi}{2} & \frac{9\pi}{4} & 3\pi & \frac{15\pi}{4} & \frac{9\pi}{2} & \frac{21\pi}{4} \end{bmatrix}\end{aligned}$$

Calculating the group delay difference

$$\tau_1 = \begin{bmatrix} \frac{3}{8} & \frac{3}{8} & \frac{3}{8} & \frac{3}{8} & \frac{3}{8} & \frac{3}{8} & \frac{3}{8} & \frac{3}{8} \end{bmatrix}$$

Creating the filter

$$H = [0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$$

Implementing the filter

$$X_{ap} \times H = Y_p = [0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$$

Performing the IFFT

$$y_p = [(\mathbf{0}) \ \mathbf{0} \ \mathbf{0} \ \mathbf{0} \ 0 \ 0 \ 0 \ 0]$$

Removing the extra N samples yields the desired result.

$$y = [(\mathbf{0}) \ \mathbf{0} \ \mathbf{0} \ \mathbf{0}]$$

The previous example shows that for one simple broadband signal the algorithm successfully returns the signal if it is within the specified pattern and removes it if not.

The algorithm was then tested with recorded audio vocal data and a square wave. The system parameters are:

Sampling Frequency $f_s = 44.1$ kHz

Frame Size $N = 2205$ samples (50 ms)

Element Spacing $l = .05$ m

Maximum Incident Angle $\theta_{\max} = 10^\circ$

Propagation Speed $c = 340.29$ m/s

The signals are 2 seconds long and are processed in N length sequential frames. Zero padding is not used because the maximum time delay between the elements ($\frac{l}{c} = 0.147$ milliseconds) is less than half of the frame size (50 milliseconds). The test signals are a 300 Hz, 50% duty cycle square wave with an amplitude of 1 (square300.wav) and a vocal sample “Now we are about to reach the end of the road”(end_of_the_road.wav). The signals used are 2 seconds in length (88200 samples).

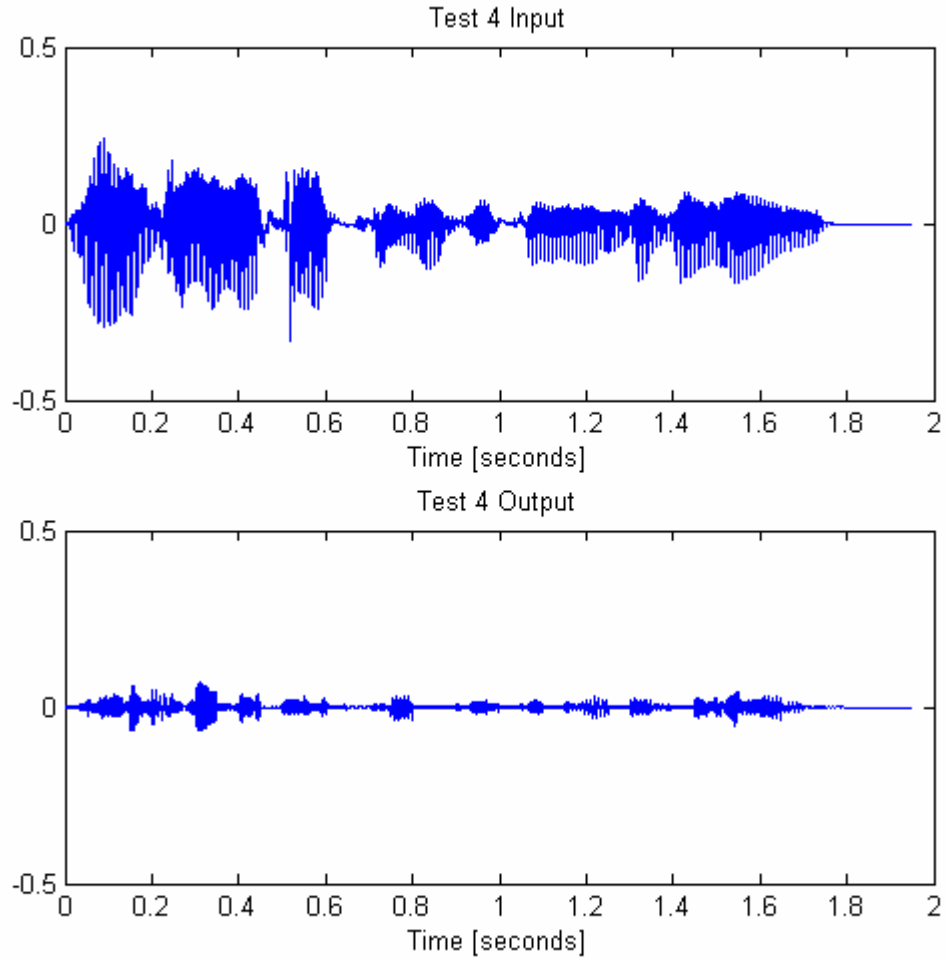


Figure 3.6. Frequency Content of Group Delay Algorithm Test Signals

The first test has the square wave arriving at zero angle of incidence. The algorithm should produce the square wave unaltered. The difference between the output and the input is on the order of 10^{-15} . The error is caused by rounding errors in the FFT/IFFT calculations. If the FFT and IFFT of the square wave are performed sequentially for the 50 ms frames, the error is identical to the error produced by the algorithm.

The second test has the square wave arriving at an angle of incidence of 30 degrees. The desired output here is zero. The actual output is a tone at 14.7 KHz which is the 49th harmonic of the 300 Hz square wave. The amplitude is 0.0204 which is the same as the amplitude of this harmonic of the square wave. This harmonic passes through the algorithm untouched because the element spacing is too large to guarantee that more than one half of a cycle of the incoming signal at 14.7 KHz can span the elements. This was expected.

The third test has the vocal sample “Now we are about to reach the end of the road.” arriving at zero angle of incidence. The algorithm should produce the unaltered sample. The difference between the output and the input is on the order of 10^{-16} . The error is caused by rounding errors in the FFT/IFFT calculations, as in test one. If the FFT and IFFT of the test signal are performed sequentially for the 50 ms frames, the error is identical to the error produced by the algorithm.

The fourth test has the vocal sample “Now we are about to reach the end of the road.” arriving at an angle of incidence of 30 degrees. The desired output here, as in the square wave case (Test 2), is zero. The algorithm does not completely eliminate the signal and creates many artifacts from the process. This can be explained by the *unwrap* function not being able to cope with rapidly changing phase values over frequency for each incoming signal. Large changes in phase may actually be different by factors of 2π or greater, but the *unwrap* function cannot compensate for jumps greater than 2π . When these phases are subtracted and differentiated, the values can be much smaller than they should be, so the

algorithm will let the corresponding frequency content through. The output can be heard in ‘Test4_output.wav’

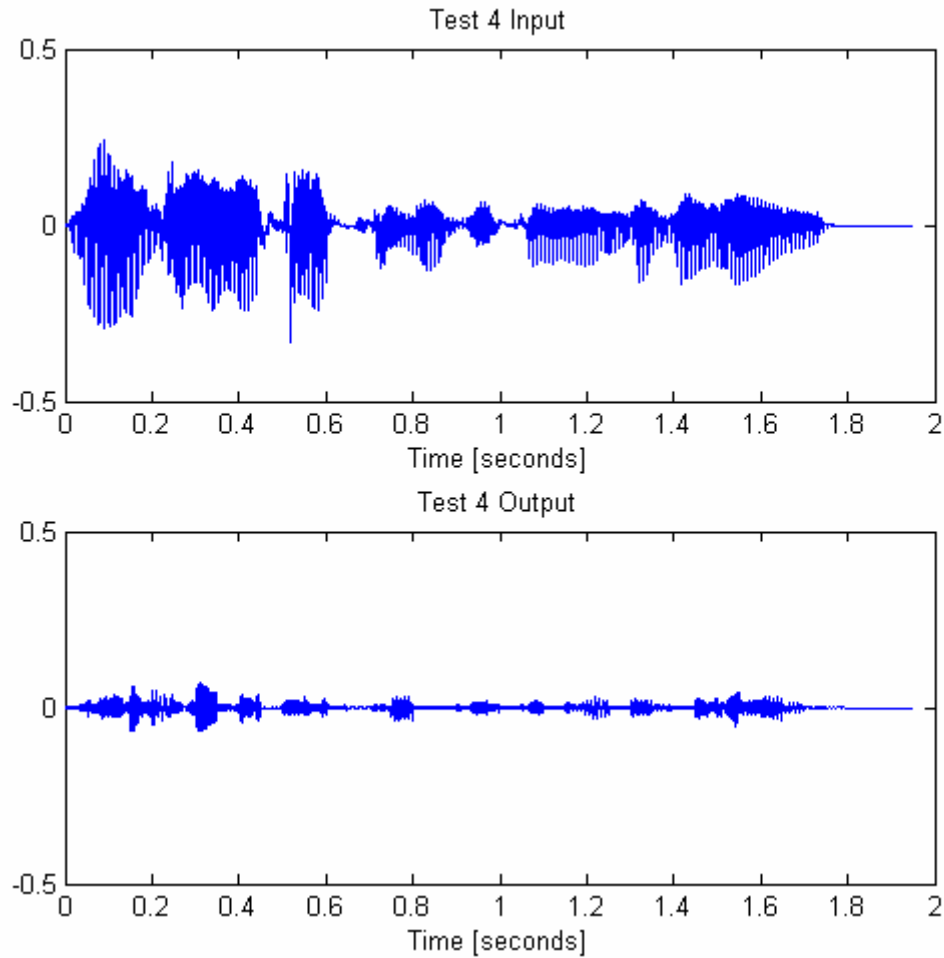


Figure 3.7. Test 4 Input and Output Comparison

Up until this point only single sources have been used in the tests. The fifth test will simulate a wanted source and interference arriving simultaneously. The vocal sample “Now we are about to reach the end of the road.” is arriving at zero angle of incidence and the square wave is arriving at an angle of incidence of 30 degrees. The input to the system at one array element can be heard in

‘Test5_input.wav’. The vocal sample is unintelligible because it is “buried” under the square wave. The algorithm should return the vocal sample and remove the square wave except where the frequency content overlaps. The actual output of the system can be heard in ‘Test5_output.wav’ and shows the power of the algorithm to remove interference. The vocal sample can be heard clearly with only the harmonic of the square wave at 14.7 kHz (as in Test 2) and a few artifacts from processing of the signal in frames.

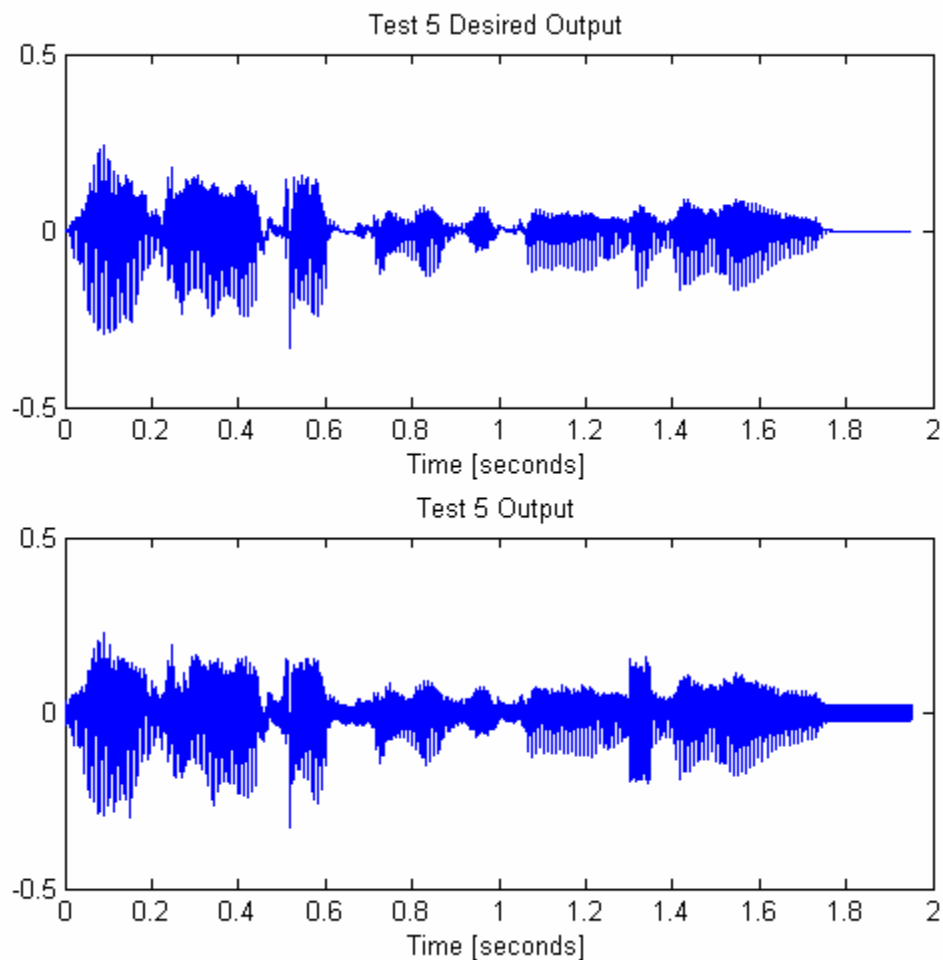


Figure 3.8. Test 5 Desired Output and Actual Output

CHAPTER 4

CONCLUSIONS

The first two techniques discussed (Frequency Up-Conversion and Non-Linear Decimation) do not prove to be useful in solving any of the problems associated with broadband beamforming, but the work done on them did provide a better understanding of the goings on in beamforming arrays. This understanding led to the design of the group delay discrimination technique.

The group delay discrimination technique meets the proposed goals by using an array much smaller (in physical size and number of elements) than traditional broadband beamforming techniques and the directivity pattern stays constant over bandwidth (if the frequency content of the signals do not overlap). In order to meet these goals, tradeoffs were made in the types of signals that can be acquired. The tradeoffs are that the frequency content of the signals cannot overlap and the phase of the signals does not change too rapidly for the algorithm to handle. If the phase discontinuity problem can be resolved, the algorithm may still work well for many of the intended applications if the frequency content of the interference does not mostly mask the frequency content of the wanted signal. If two speakers (one wanted and one unwanted) have different voice profiles the algorithm should distinguish between the two.

The group delay discrimination technique can be improved and expanded upon by further research into:

- Using an improved algorithm to “unwrap” the phase information.
- Processing more than two sensors for larger bandwidth performance.
- Processing more than two sensors for three dimensional pickup patterns.
- Improving the filter creation algorithm to create more complex beamforms.

Further research into the uses of the group delay discrimination technique can include but is certainly not limited to direction finding and source localization for both acoustic and electromagnetic sources. The group delay discrimination algorithm was developed for use in audio-band acoustics, but like beamforming in general, it can be applied to a number of different fields and is certainly not limited to acoustics.

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APPENDIX

Audio Files from Group Delay Discrimination Testing:

‘square300.wav’

‘end_of_the_road.wav’

‘TEST4_output.wav’

‘TEST5_input.wav’

‘TEST5_output.wav’

Matlab Function which Performs Grpup Delay Discrimination Algorithm:

‘discrim.m’

VITA

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